

Solution of combined economic emission dispatch by hybrid TLBO-SQP

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Abstract

“TEACHING LEARNING BASED OPTIMIZATION--SEQUENTIAL QUADRATIC PROGRAMING” is a budding efficient hybrid optimization Technic which is proposed in this paper as a tool to optimize the Combined Economic Emission Load Dispatch Problem in Electrical Power System . The key mechanism of this optimization method is that the solution found by TLBO is fine-tuned by SQP . . Being a population based optimization technic, this method utilizes a population of solutions for heading towards global solution which is taken as input to SQP.The Algorithm has been experimented on three different test systems and the superiority has been revealed in comparison to some other optimization technics.

Key word: optimization, TLBO ,SQP, Load dispatch,

1 Introduction

Combined Economic Emission Dispatch of load is the most recent optimization problem of power system which can be solved by classical as well as modern optimization techniques. Classical techniques are keen to converge to a local optima and incapable of handling large number of inequality constrains. Modern evolutionary optimization technique like PSO, GA, EP, ABC. TLBO etc are also applied to solve CEED problem. It has been found that among them TLBO gives better results in terms of computational time. But these methods have the problem of premature convergence in their performance. In this context, Various hybrid methods have been applied to solve CEED . These hybrid optimization methods were found to be more effective and accurate, In this paper

a hybrid technique of optimization involving TLBO and SQP is developed . SQP is one of best nonlinear-programming method for constrained optimization.

2. Overview of CEED COMBINED ECONOMIC EMISSION DISPATCH PROBLEM

2.1 Problem Description

The optimum economic dispatch cannot handle the environmental criteria. By proper load allocation among the various generating units of the plants, harmful ecological effects by the emission of gaseous pollutants like NO_x , SO_x , from fossil fuel power plants can be reduced But this load allocation may cause increasing in the operating cost of the generating units. So, a solution which gives a balanced result between emission and cost should be found out. This is achieved by solving combined economic emission dispatch problem. This dual-objective CEED problem is converted into a single objective function using a price penalty factor approach

3. Objective Function

: The combined Economic Emission Dispatch is a bi-objective Problems which is converted to a single one by a cost penalty factor or hybridization factor as

$$f(P_{Gi})= \text{Min} \sum_{i=1}^{nG} [F_i(P_{Gi}), E_i(P_{Gi})] \quad (1)$$

where $f(P_{Gi})$ is the optimal cost of power generation, $F_i(P_{Gi})$ and $E_i(P_{Gi})$ are total cost and total emission, nG is the number of generators . The constraints are

$$\sum_{i=1}^{nG} P_{Gi} = P_D - P_L \text{ where}$$

P_{Gi} , is the real power generation of ith generator, P_D and P_L are total load and transmission loss of the system

$$P_{Gi}^{min} \leq P_{Gi} \leq P_{Gi}^{max} \text{ where}$$

P_{Gi}^{min} and P_{Gi}^{max} are minimum and maximum real power allowed at generator i respectively

The fuel cost of production $F_i(P_{Gi})$ (Rs/hr) can be expressed as in terms of control variable

$$F_i(P_{Gi}) = \sum_{i=1}^{nG} (a_i P_{Gi}^2 + b_i P_{Gi} + c_i) \quad (2)$$

Where

P_{Gi} is the real power output in ith generator, a_i, b_i and c_i are fuel cost curve coefficient

The total function of emission $E_i(P_{Gi})$ (kg/hr) can be expressed as

$$E_i(P_{Gi}) = \sum_{i=1}^{nG} (\alpha_i P_{Gi}^2 + \beta_i P_{Gi} + \gamma_i) \quad (3)$$

Where α_i, β_i and γ_i are emission coefficient

The factor of Hybridization is

$$H_I = \sum_{i=1}^{nG} F_i(P_{Gi}^{Max}) / \sum_{i=1}^{nG} E_i(P_{Gi}^{Max})$$

Where $i=1,2,3,\dots,nG$

The function to be minimized can be described as

$$\text{Min } \{f(P_{Gi}) = \sum_{i=1}^{nG} F_i(P_{Gi}) + H_I * \sum_{i=1}^{nG} E_i(P_{Gi})\}$$

Subject to equality constraints

$$\sum_{i=1}^{nG} P_{Gi} - P_D - P_L = 0 \quad (4)$$

And in equality constraints

$$P_{Gi}^{Min} \leq P_{Gi} \leq P_{Gi}^{Max} \quad (5)$$

To handle the constraints, the violated constraints are squared then multiplied by a penalty coefficient and add to the fitness function

$$\text{Min} F(x) \text{ subject to } g(x) \leq 0 \quad h(x) = 0$$

The constrained function $f(x)$ can be transformed to un constrained function $F(x)$

$$\text{Min } F(x) = f(x) + r_p [(\max(0, g(x)))^2 + h(x)^2] \quad (6)$$

Where r_p penalty coefficient

For application of GA the problem can be as

$$F(P_{Gi}, r_p) = f(P_{Gi}) + r_p * [\sum_{j=1}^m (h_j(P_{Gi}))^2 + \sum_{q=1}^k (g_q(P_{Gi}))^2] \quad (7)$$

Equality constraints $h_j(P_{Gi}) = 0, j = 0, 1, \dots, m$

Inequality constraints $g_q(P_{Gi}) \leq 0, q = 0, 1, \dots, k$

The following steps are used to find the price penalty factor for a particular load demand:

1. Find the ratio between maximum fuel cost and maximum emission of each generator
2. Arrange the values of price penalty factor in ascending order.
3. Add the maximum capacity of each unit ($P_{i,lu}$) one at a time. starting from the smallest h , until $P_{i,lu} > P_{,}$.
4. At this stage, h , associated with the last unit in the process is the price penalty factor h for the given load.

The above procedure gives the approximate value of price penalty factor

computation for the corresponding load demand. Hence a modified price penalty factor (h_i) is used to give the exact value for the particular load demand. The first two steps of h_i computation remain the same for the calculation of modified price penalty factor. Then it is calculated by interpolating the values of h_i , corresponding to their load demand values.

4. Overview of Teaching Learning Based Optimization Technic (TLBO)

TLBO method is a relationship based method between teacher and students in the class. The method is analogous to the effect of teacher students understanding learning in a class

The population in TLBO is a group of Learners.

TLBO consists of two parts

- i) “TEACHER PHASE”
- ii) “LEARNER PHASE”

Initialization of the population is random within certain limit and the concerned equation is

$$X_{i,j}^0 = X_j^{min} + rand * (X_j^{max} - X_j^{min}) \text{-----}(3)$$

Where $rand$ denotes uniformly distributed random variable within the range (0,1),

X_j^{min}, X_j^{max} = minimum and maximum value of j th parameter

- i) Teacher phase:

The mean parameter of each subject of the learners in the class at generator g is given by

$$M^g = [m_1^g, m_2^g, \dots, m_j^g, \dots, m_D^g] \text{-----}$$

To obtain a new population set of learner

$$X_{new_i}^g = X_i^g + rand(X_{Teacher}^g - T_F * M^g) \text{-----(4)}$$

T_F =Teaching factor between value 1 to 2

If $X_{new_i}^g$ is better than X_i^g in generation g then it replace X_i^g otherwise wise it remains X_i^g

ii) Learner Phase

The students can enhance their knowledge in Learner Phase by interacting with other students or by sharing knowledge

For a Learner X_i^g

Another learner X_r^g is randomly selected with $i \neq r$

Now to set a new vector in learner phase

$$X_{new_i}^g = X_i^g + rand * (X_i^g - X_r^g) \text{ if } f(X_i^g) < f(X_r^g) \text{-----(5)}$$

$$X_{new_i}^g = X_i^g + rand * (X_r^g - X_i^g) \text{ if } f(X_i^g) > f(X_r^g) \text{-----(6)}$$

5. Overview of sequential quadratic programming

Out of a number of nonlinear programming method of optimization, SQP Method is very much handy for constrained optimization problem. SQP iteratively approximate the Nonlinear Programming problem by a sequence of Quadratic Programming sub problem.[5] . The quadratic sub problem is formulated to have result of sequence of solutions converge to a local optimum of NLP.It is one of the best in terms of efficiency, accuracy and percentage of successful solution over a large number of test problems. IT is similar to Newton’s method for constrained optimization. Broyden –Fletcher-Goldfarb-Shanno quasi-Newton updating method is utilized to make an approximation of Hessian of the Lagrangian function. Quadratic programming sub problem is formulated by using the result of the

above approximation. The solution of the sub problem create a search direction for a line search procedure .CEED is a non convex and no smooth function, SQP gives a local minima initially. In this paper TLBO is used as a global search and the best solution of TLBO is taken as initial condition for SQP method for fine tune solution which is a local minima.

Consider the application of the SQP methodology to nonlinear optimization problems,

Min. $f(x)$

Subject to

$h(x)=0$

$g(x)\leq 0$

The Lagrangian of this problem can be written as,

$L(x,\lambda,\mu)=f(x)+\lambda h(x)+\mu^T g(x)$

where λ and μ are vectors of multipliers. SQP is an iterative procedure which models the problem for a given iterate x_k by a quadratic programming sub-problem, solves that quadratic programming sub-problem, and then uses the solution to construct a new iterate x_{k+1}

The sub problem can be constructed by linearizing the constraints around x_k as follows

$$\text{Min } \nabla f(x^k)(x-x^k) + \frac{1}{2}(x-x^k)^T Hf(x^k)(x-x^k)$$

Where H is the Hessian matrix.

Subject to

$$h(x^k) + \nabla h(x^k)(x-x^k) = 0$$

$$g(x^k) + \nabla g(x^k)(x-x^k) \leq 0$$

We need to update the multipliers in a corresponding search direction and choose a step size to evaluate the next iterate.

6. TLBO-SQP applied to CEED

The hybrid TLBO-SQP algorithm is applied to solve combined economic emission dispatch for optimal fuel cost and emission. The TLBO is used to find a near global solution and SQP is used as a local search to determine the optimal solution at the final.

The sequential steps involved in solution of CEED by TLBO-SQP are as explained below

Step 1: Input the total number of learners, number of subjects offered to the learners, cost coefficients, loss coefficients, load demand and limits of the constraints. Here the number of learners in a class is considered as population and the number of subjects offered to the learner is considered as generators..

Step 2: Generate the initial population which satisfies the limits and constraints..

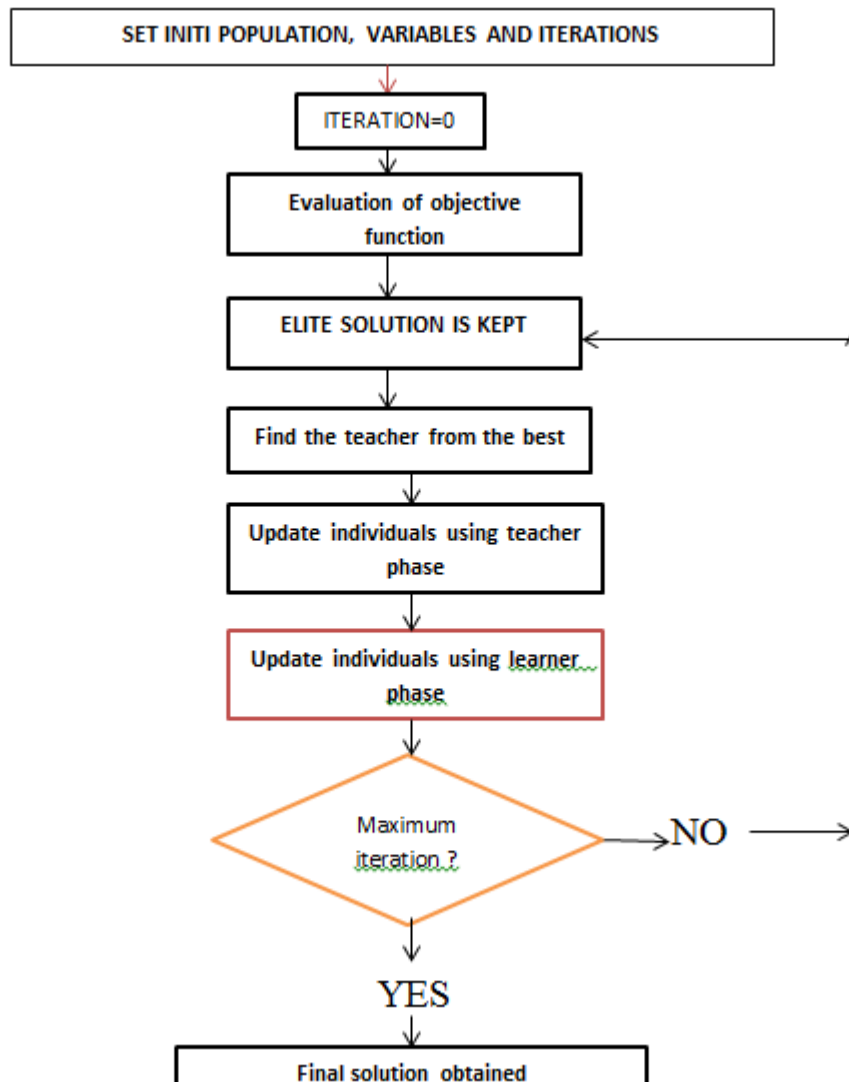
Step 3: Objective function of each individual is calculated.

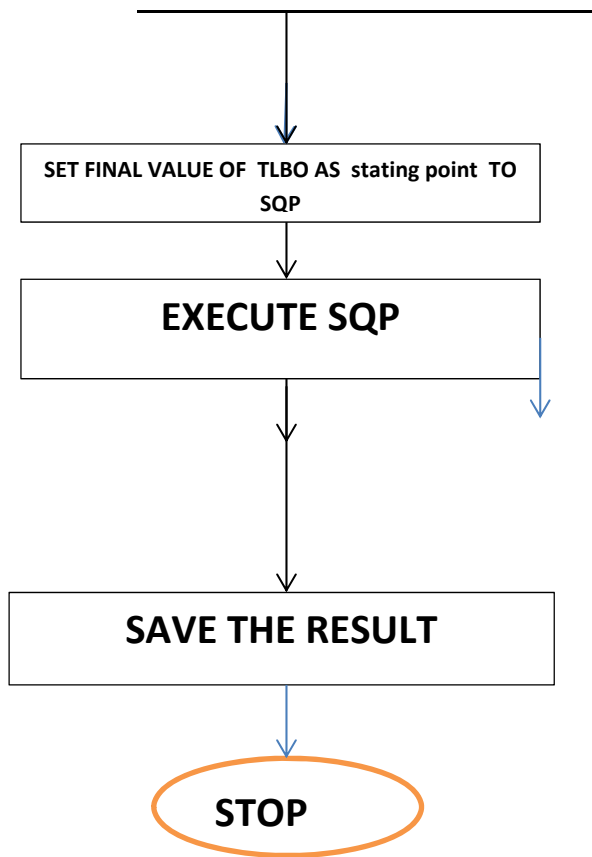
Step 4: : In the current iteration the best solution is considered as the teacher and the new value of population is generated in the teacher phase. If any new individual violates the limit set that individual at the limiting value. If the equality constraint is violated, discard that individual and repeat the process until all constraints are satisfied.

Step 5: New learners are evaluated in learner phase. If any new individual violates the limit set that individual at the limiting value. If the equality constraint is violated, discard that individual and repeat the process until all constraints are satisfied.

Step 6: Check for termination criteria. If the termination criterion is met go to step 7 otherwise repeat from step 4.

Step 7: Apply the solution obtained from step 6 of TLBO as initial point of SQP and solve the SQP. Here the SQP method will be used to fine-tune the improving (better fitness) solution





8. Results and Discussion

The proposed SQP TLBO algorithm is applied to solve ELD, EED and CEED for three different test cases.

Test case 1: 6 unit system

Test case 2: 10 unit System

Test case 3: 13 unit System

. Test case 1

Table 6.1

Generator	Economic load dispatch by TLBO	Economic load dispatch by GA-	Economic load dispatch by
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		TLBO	SQP-TLBO
PG1	0.129	0.127	0.127
PG2	0.298	0.299	0.298
PG3	0.455	0.453	0.454
PG4	1.122	1.1175	1.1175
PG5	0.52	0.5290	0.5290
PG6	0.314	0.3146	0.3146
FUEL COST	602.406	602.404	602.402
EMISSION	0.2302	0.2299	0.2299

Table 6.2

Generator	Economic Emission dispatch by TLBO	Economic Emission dispatch by GA-TLBO	Economic Emission dispatch by SQP-TLBO
PG1	0.411	0.4099	0.4099
PG2	0.477	0.4721	0.4721
PG3	0.548	0.5456	0.5456
PG4	0.384	0.3955	0.3955
PG5	0.548	0.5387	0.5387
PG6	0.518	0.5239	0.5239
FUEL COST	651.14	650.05	650.05
EMISSION	0.194	0.1942	0.1942

Table 6.3

Generator	CEED by TLBO	CEED by GA-TLBO	CEED by SQP-TLBO
PG1	0.259	0.255	0.256
PG2	0.281	0.361	0.361
PG3	0.632	0.636	0.637
PG4	0.724	0.743	0.743

PG5	0.592	0.479	0.479
PG6	0.381	0.39	0.3899
FUEL COST	616.001	615.01	614.97
EMISSION	0.2044	0.204	0.2036

The results of solution ELD, EED and CEED by SQP-TLBO for 6 unit system are given in Table 6.1, 6.2 and 6.3 respectively. Results obtained by TLBO and GA-TLBO are also shown for comparison. Table 6.1 depicts that the fuel cost in case of ELD for 6 unit system obtained by TLBO, GA-TLBO and SQP-TLBO are 602.406\$, 602,404\$ and 602.402\$ respectively which clearly reveals the fact that fusion of SQP with TLBO gives better performance. Similar kind of result is observed for EED and CEED as well.

Test case 2

Table 6.4

Generator	Economic load dispatch by TLBO	Economic load dispatch by GA-TLBO	Economic load dispatch by SQP-TLBO
PG1	55	40.5326	40.5326
PG2	79.999	45.8383	45.8383
PG3	106.946	115.7578	115.7578
PG4	100.607	104.3776	104.3776
PG5	81.478	104.7259	104.7259
PG6	83.007	112.6931	112.6931
PG7	299.999	285	284.9527
PG8	339.999	252.21	251.1221
PG9	469.999	470.00	470.00
PG10	469.999	470.00	470.00
FUEL COST	111497.632	108015.0	107049.0
EMISSION	4572.362	4123.7	4118.29

Table 6.5

Generator	Economic Emission dispatch by TLBO	Economic Emission dispatch by GA-TLBO	Economic Emission dispatch by SQP-TLBO
PG1	55	55	55
PG2	80	80	80
PG3	81.134	82.13	81.13
PG4	81.363	81.36	81.36
PG5	160	81.5	81.5
PG6	240	160	160
PG7	294.485	240	240
PG8	297.27	295.48	294.48
PG9	396.77	396.76	396.76
PG10	395.576	395.57	395.57
FUEL COST	116412.443	116512.44	116412.44
EMISSION	3932.243	3932.24	3932.24

Table 6.6

Generator	CEED by TLBO	CEED by GA-TLBO	CEED by SQP-TLBO
PG1	54.888	46.49749	46.49749
PG2	79.96	75	73.58246
PG3	86.586	75.37136	75.37136
PG4	83.74	63.07534	63.07534
PG5	134.27	99.64559	99.64559
PG6	157.134	240.0000	240.0000
PG7	297.64	227	226.8554
PG8	217.295	340.0090	340.0090
PG9	440.48	470.0000	470.0000
PG10	432.23	364.9724	364.9724

FUEL COST	113106.894	110421.605	110337.605
EMISSION	4150.496	3922.49	3908.49

The results of solution ELD, EED and CEED by SQP-TLBO for 10 unit system are shown in Table 6.4, 6.5 and 6.6 respectively. Results obtained by TLBO and GA-TLBO are also given for comparison.

Table 6.4 depicts that the fuel cost in case of ELD for 10 unit system obtained by TLBO, GA-TLBO and SQP-TLBO are 111497.632 \$, 108015.0\$ and 107049.0 \$ respectively which clearly reveals the fact that fusion of SQP with TLBO gives better performance. Similar kind of result is observed for EED and CEED as well.

Test case 3

Table 6.7

Generator	Economic load dispatch by TLBO	Economic load dispatch by GA-TLBO	Economic load dispatch by SQP-TLBO
PG1	628.32	628.32	628.32
PG2	222.75	222.75	222.75
PG3	149.6	149.6	149.6
PG4	109.87	109.87	109.87
PG5	60	60	60
PG6	109.87	109.87	109.87
PG7	109.87	109.87	109.87
PG8	109.87	109.87	109.87
PG9	109.87	109.87	109.87
PG10	40	40	40
PG11	40	40	40
PG12	55	55	55
PG13	55	55	55

FUEL COST	17963.83	17963.83	17963.83
EMISSION	461.48	461.48	461.48

Table 6.8

Generator	Economic Emission dispatch by TLBO	Economic Emission dispatch by GA-TLBO	Economic Emission dispatch by SQP-TLBO
PG1	80.64	80.64	80.64
PG2	166.33	166.33	166.33
PG3	166.33	166.33	166.33
PG4	154.73	154.73	154.73
PG5	154.73	154.73	154.73
PG6	154.73	154.73	154.73
PG7	154.73	154.73	154.73
PG8	154.73	154.73	154.73
PG9	154.73	154.73	154.73
PG10	119.96	119.96	119.96
PG11	119.96	119.96	119.96
PG12	109.19	109.19	109.19
PG13	109.19	109.19	109.19
FUEL COST	19145.57	19145.57	19145.57
EMISSION	58.24	58.24	58.24

Table 6.9

Generator	CEED by TLBO	CEED by GA-TLBO	CEED by SQP-TLBO
PG1	179.20	180	179.025
PG2	224.73	224.13	224.13
PG3	299.21	298.44	298.44
PG4	159.61	160	159.73

PG5	109.87	159.73	159.73
PG6	159.72	159.74	159.74
PG7	159.64	159.70	159.70
PG8	159.74	159.63	159.63
PG9	158.04	109.86	109.86
PG10	40.01	40	40
PG11	40	40	40
PG12	55	55	55
PG13	55.11	55	55
FUEL COST	18047.063	18041.84	18038.84
EMISSION	85.8	85.695	85.65

The results of solution ELD, EED and CEED by SQP-TLBO for 13 unit system are shown in Table 6.7, 6.8 and 6.9 respectively. Results obtained by TLBO and GA-TLBO are also given for comparison.

. Table 6.7 depicts that the fuel cost in case of ELD for 13 unit system obtained by TLBO , GA-TLBO and SQP-TLBO are 17963.83 \$, 17963.83 \$ and 17963.83 \$ respectively which clearly reveals the fact that fusion of SQP with TLBO gives better performance. Similar kind of result is observed for EED and CEED as well.

Summary

6 UNITS						
	FUEL COST			EMISSION		
ECONOMIC LOAD DISPATCH	TLBO	GA-TLBO	SQP-TLBO	TLBO	GA-TLBO	SQP-TLBO
	602.406	602.404	602.402	0.2302	0.2299	0.2299
ECONOMIC EMISSION DISPATCH	651.14	650.05	650.05	0.194	0.1942	0.1942
CMBINED ECONOMIC	616.001	615.01	614.97	0.2044	0,204	0.2036

EMISSION DISPATCH						
10 UNITS						
ELD	111497.632	108015.0	107049.0	4572.362	4123.7	4118.29
E E D	116412.443	116512.44	116412.44	3932.243	3932.24	3932.24
CEED	113106.894	110421.605	110337.605	4150,496	3922.49	3908.49
13 UNITS						
ELD	17963.83	17963.83	17963.83	461.48	461.48	461.48
E E D	19145.57	19145.57	19145.57	58.24	58.24	58.24
CEED	18047.063	181041.84	18038.84	85.8	85.695	85.65

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