

Image Compression by DWT and DTCWT Using an SPIHT Algorithm

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Abstract

The objective of compression is to cut back irrelevancy associate in nursing redundancy of the image information so as to be able to store or transmit information in an economical type. In engineering science and knowledge theory, compression is that the method of secret writing data victimization fewer bits than the first illustration would use. Compression is beneficial as a result of it helps cut back the consumption of high-priced resources, like disc house or transmission information measure. Technological advances and therefore the advent of the net, image files became one amongst the foremost common file sorts to be used and shared these days. however at the side of their convenience, image files square measure typically massive, creating them tough to store and transmit. to beat this The Dual-tree complex wavelet transform (DTCWT) could be a comparatively recent sweetening to the discrete wavelet transform (DWT), with necessary further properties. It achieves this with a redundancy issue of solely 2nd for d-dimensional signals, that is considerably not up to the undecimated DWT. The DTCWT introduced by Kingsbury, is close to shift-invariant and provides directional analysis in 2-D and better dimensions. A brand new compression rule that's supported DT-CWT and SPIHT is conferred. Approximate shift unchangeableness, smart directional property procedure potency properties of DT-CWT build it a decent candidate for compression. A changed SPIHT rule is introduced so as to extend its potency for compression. To raised shield the host options and increase the lustiness of the watermark, the dual-tree complex wavelet transform (DT-CWT) is employed.

Keywords: WT, DWT, DTCWT, SPIHT algorithm

1. Introduction

Wavelet transform (WT): Is predicated on wavelets. It's wont to analyze a symbol (image) into totally different frequency parts at different resolution scales (i.e. multiresolution). This permits revealing pictures spacial and frequency attributes at the same time. Mounted resolution limitation of STFT will be resolved by material possession the resolution t and f vary in time-frequency plane so as to obtain Multiresolution analysis. The wave let transform in

its continuous (CoWT) kind provides a versatile time-frequency window, that narrows once perceptive high frequency phenomena and widens once analyzing low frequency behaviour. The wave transformation could be a mathematical tool for decomposition. The Wavelet transform is similar to a gradable sub band filtering system, wherever the sub bands square measure logarithmically spaced in frequency. The essential plan of the DWT for a two-dimensional image is delineate as follows. a picture is initial rotten into four elements supported frequency sub bands, by critically sub sampling horizontal and vertical channels exploitation sub band filters and named as Low-Low (LL), Low-High (LH), High- Low (HL), and High- High (HH) sub bands as shown in figure

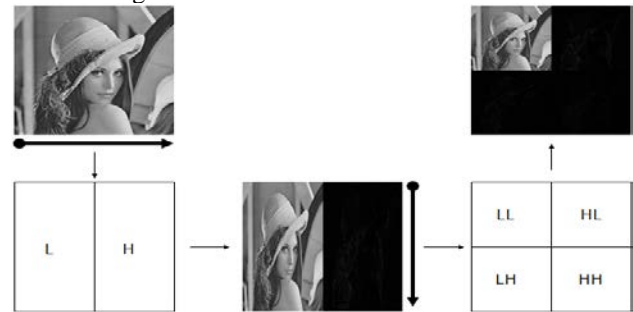


Fig 1: Discrete Wavelet Decomposition

Discrete Wavelet Transform:

Discrete Wavelet Transform (DWT) is with efficiency employed in Image cryptography applications attributable to their information reduction capabilities. The multiresolution nature of the separate ripple remodel is tried as a robust tool to represent pictures rotten on the vertical and horizontal directions exploitation the pyramidic multiresolution theme. Compression algorithms supported DWT offer high cryptography potency for natural (smooth) pictures, the quality DWT has 3 major disadvantages that weaken its application. This dis-blessings area unit represented as below:

Lack of shift invariance: It implies that little shifts within the signaling will cause hit or miss modification within the distribution of energy between DWT coefficients at totally different scales. It's been determined that the quality DWT is seriously deprived by the shift sensitivity that arises from down samplers within the DWT implementation.

Poor directional selectivity: Once the m-Dimensional remodel ($m \geq 1$) coefficients reveal solely a number of feature orientations within the spacial domain,
 Absence of section Information: Section info is effective in several signal process applications like in image compression and power measure e.g. For a fancy valued signal or vector, its section is computed by its real and notional projections. Digital image could be a information matrix with a finite support in 2-D. Process the image with 2-D DWT will increase section size and adds section distortion.

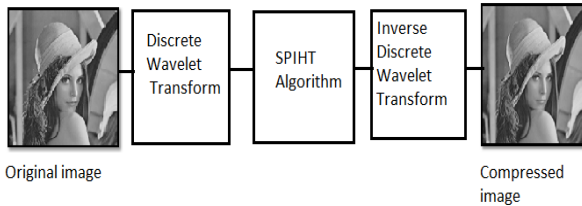


Fig 2: Method of Image Compression scheme

As dyadic DWT doesn't adapt to the assorted house frequency properties of pictures, the energy compaction it achieves is usually not optimum. However, the performance will be improved by choosing the remodel basis adaptively to the image.

Dual Tree Complex Wavelet Transform (DTCWT):

Recent developments in advanced riffle Transforms are classified into 2 necessary categories, Redundant CWT (RCWT), and Non-Redundant CWT (NRCWT). The necessary sorts of RCWT embrace Kingsbury's. These redundant transforms encompass 2 typical DWT filter bank trees operating in parallel with several filters of each the trees in approximate construction to get real and {imaginary part of complex riffle coefficients. This introduces restricted redundancy and permits the remodel to supply approximate shift variance and directionally selective filters whereas protective the same old properties of good reconstruction and procedure potency with sensible well balanced frequency responses.

Redundant Complex Wavelet transforms:

The RCWT embrace 2 nearly similar CWTs. They're denoted as DT-DWT (Dual-Tree DWT based mostly CWT) with 2 nearly similar versions specifically Kingsbury's DTDWT (K), and Selesnick's DT-DWT(S). These redundant transforms encompass 2 typical DWT filterbank trees operating in parallel with several filters of each the trees in approximate construction. The filterbank structure of each DT-DWTs is same as that of DWT however the planning strategies to get the filter coefficients are completely different. Each DT-DWTs offer part information; they're shift-invariant with improved directivity. Selesnick planned an alternate filter

style strategies for DT-DWT (K) and designed DT-DWT(S), nearly appreciate DT-DWT (K) specified within the limit the scaling and riffle functions type mathematician remodel pairs. DT-DWT(S) is meant with straightforward strategies to get filter coefficients.

KINGSBURY'S Dual Tree-DWT (DT-DWT(K))

It is ascertained that approximate shift changelessness is feasible with normal DWT by doubling the rate at every level of the tree. For this to figure, the samples should be equally spaced and down samplers should be eliminated when the level-1 filters. this can be appreciate having 2 parallel absolutely decimated trees, real (tree-a) and fanciful (tree-b) as in figure if the delays of initial level filters of tree-b ar one sample offset by their corresponding filter in tree-a. This offset ensures the pickup of opposite samples in each trees to urge uniform interval between the samples of each trees when level-1, filters in one tree should offer delays that are $[*fr1]$ a sample completely different from those in opposite tree.

The DT-DWT (K) will be designed in 2 ways in which to own needed delays. The primary relies on odd-even length filters and also the second employs Q-shift (quarter shift) filter style. The key issue within the style of DT-DWT (K) is to get (approximate) shift changelessness victimization any of the filter forms

The main issues with the odd/even filter approach to achieving this delay are that:

- The sub-sampling structure isn't terribly symmetrical.
- The 2 trees have a rather completely different frequency responses.
- The filter sets should be bi-orthogonal as a result of they're linear part.

These drawbacks are overcome with a newer kind of twin tree referred to as a Q-shift dual tree.

Q-shift filters

There are 2 sets of filters used, the filters at level one, and also the filters the least bit higher levels. The filters on the far side level one have even length however are not any longer strictly linear part. Instead they're designed to own a gaggle delay of roughly $\frac{1}{4}$. The required delay distinction of $\frac{1}{2}$ sample is achieved by victimization the time reverse of the tree a filters in tree b. The PR filters used are chosen to be orthonormal, so there construction filters are simply the time reverse of the equivalent analysis filters. There are variety of decisions of attainable filter combinations. The Q-shift remodel retains the nice shift changelessness and directivity properties of the first whereas conjointly up the sampling structure.

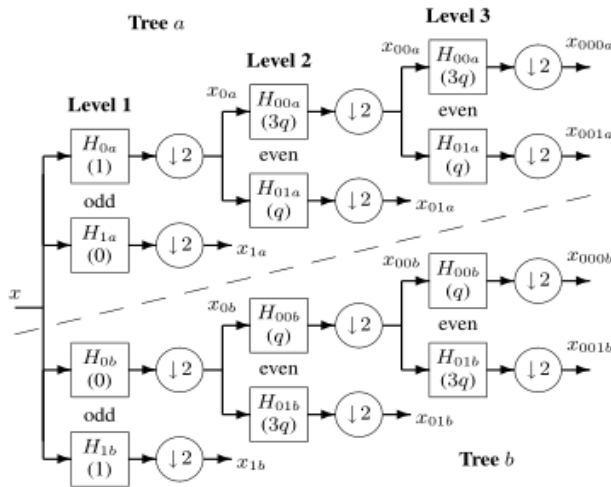


Fig 3: Q Shift filter – Dual Tree Complex Wavelet Transform over 3 level

The main benefits as compared to the DWT square measure that the advanced wavelets square measure close to shift invariant which the advanced wavelets have separate subbands for positive and negative orientations. standard severable real wavelets solely have subbands for 3 totally different orientations at every level and can't distinguish lines close to forty five from those close to -45. The Advanced CWT attains these properties by commutation the tree structure of the standard wavelet transform with a twin tree. At every scale one tree produces the important a part of the advanced ripple coefficients, whereas the opposite produces the fanciful elements. necessary that each one the filters within the twin tree square measure real. Advanced complex coefficients solely seem once the 2 trees measure combined.

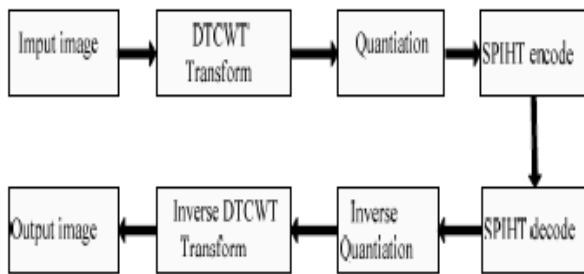


Fig 4: Dual Tree Complex Wavelet Transform Process Flow

Algorithm

Why SPIHT Algorithm?

The SPIHT (Set Partitioning in hierarchal Tree) technique isn't an easy extension of ancient ways for compression and represents a crucial advancement within the field. The

strategy deserves special attention as a result of it provides the following:

- _ Good image quality and high PSNR
- _ It's optimized for progressive image transmission
- _ Turn out totally embedded code file
- _ Simple quantisation algorithmic program
- _ It will code to precise bit rate or distortion
- _ It is used for lossless compression
- _ Economical combination with error protection

SPIHT Algorithm:

The SPIHT image cryptography algorithmic program was developed in 1996 by same and Pearlman and is another a lot of economical implementation of the embedded zero tree ripple (EZW) algorithmic program by Shapiro. Developed a quicker and a lot of economical image cryptography technology referred to as Set Partitioning in hierarchal Trees (SPIHT). Some of the most effective results that acquire highest PSNR values for given compression ratios for a good form of pictures are obtained with SPIHT. To change the SPIHT computer user there square measure two ideas for the SPIHT cryptography procedures. First, within the original SPIHT cryptography method, a lesser range of bit planes square measure discarded for higher target bit-rates. Inversely, a lot of bit-planes square measure discarded for lower target bit-rates. If we are able to confirm the connection between the bit-planes and target bit-rates, we are able to straightaway discard the suitable of bit-planes to realize totally different target bit-rates. Second, at low bit-rates (implying that some bit-planes square measure to be discarded), if a sub-band constant is slightly not up to $2n$ and significantly larger than $2(n-1)$, we must always then regard the constant as being important, and one bit is employed to explain its significance. it's apparent that the opposite LSB bit-planes don't seem to be coded and also the compression rate is improved. once the wavelet transform is applied to a picture, the most algorithmic program works by partitioning the wavelet decomposed into important and insignificant partitions supported the subsequent operate

$$S_n(T) = f(x) = \begin{cases} 1, & \max_{(i,j)} eT\{ |C_{ij}| \} \geq 2^n \\ 0, & \text{otherwise} \end{cases}$$

Where,

$S_n(T)$, is the significance of a set of co-ordinates T,

Algorithm - Sorting pass and Refinement pass

Sorting pass is performed on the list of insignificant sets (LIS), list of insignificant pixels (LIP) and also the list of serious pixels (LSP). The LIP and LSP include nodes that contain single pixels, whereas the LIS contains nodes that

have descendants. The most range of bits needed to represent the biggest constant within the spacial orientation tree is obtained and selected as nmax. Throughout the sorting pass, those co-ordinates of the pixels that stay within the LIP square measure tested for significance by victimisation eqn. 2. The result, S,(T), is distributed to the output. Those that measure important are transferred to the LSP moreover as having their sign bit output. Sets within the LIS (which consists of nodes with descendants will have their significance tested and, if found to be important, are removed and divided into subsets. Subsets with one constant and located to be important are side to the LSP or else they're going to be side to the LIP.

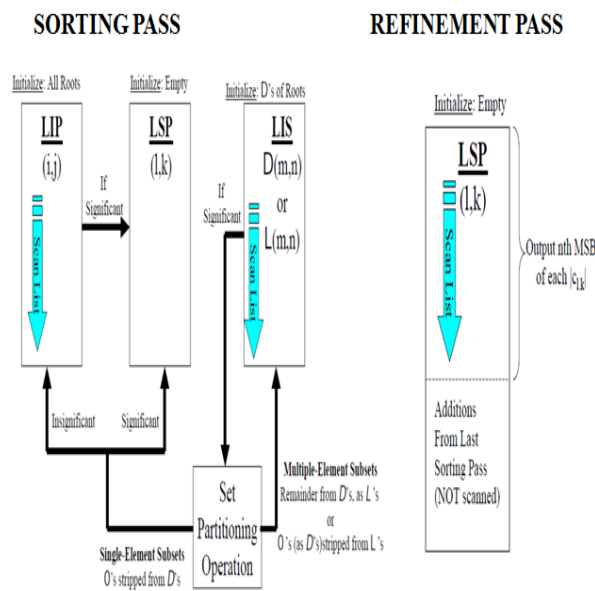


Fig: Sorting and Refinement pass scheme

During the Refinement pass, the ordinal most vital little bit of the coefficients within the LSP is output. The worth of n is reduced by one and also the sorting and refinement passes square measure continual. This continues till either the required rate is reached or n =0, and every one the nodes within the LSP have all their bits output. The latter case can end in nearly excellent reconstruction of time interval.

The significance data is hold on in three ordered lists: LIS, LIP, LSP

Each list entry is known by a coordinate (i,j); within the LSP the coordinate represents either D(i,j) or L(i,j). Throughout the Sorting path: Pixels is LIP tested and people that become important square measure side to the LSP.

_ Sets in LIS square measure consecutive evaluated; important sets square measure divided and new subsets square measure side to LIS, LIP or LSP.

_ Pixels is LSP square measure visited within the refinement pass.

_Both encoder and decoder use a similar algorithmic program. sensible experiments have shown there's very little to be gained by entropy-coding algorithms output.

_ There's applied mathematics dependence between significance of adjacent pixels, which might be exploited by victimisation the adaptive arithmetic cryptography to extend cryptography potency.

Results:

The results of the compression victimisation DWT and DTCWT pictures are given within the tables one and tables two. The performance measures for numerous signals square measure evaluated by mean sq. error (MSE) as in equation (1) and peak signal to noise quantitative relation (PSNR) as in equation (2).

$$\sigma^2 = \frac{1}{MN} \sum_{i=0}^{M-1} \sum_{j=0}^{N-1} (x_{ij} - \hat{x}_{ij})^2 \text{ ----- (1)}$$

$$PSNR = -20 \log_{10} \frac{255}{\sigma^2} \text{ ----- (2)}$$

CR=original image size in bits / compressed image size in bits, wherever M x N is that the image size and p is that the bits per picture element, x i,j is that the original image and x' i,j is that the reconstructed image.

Conclusion:

It is clear from the performance results of table (1), associated table (2) that the compression capability of DTCWT with an SPIHT algorithmic program (namely DT-DWT (K)) is superior than the DWT.

TABLE 1: PERFORMANCE MEASURES: PSNR

Images	PSNR	
	DWT	DTCWT
Lena	32.0166	54.2791
Rose	56.7357	56.7603
Cameraman	52.6128	55.5434

DWT

DTCWT

TABLE2: PERFORMANCE MEASURES:
 COMPRESSION RATIO

Images	Compression Ratio	
	DWT	DTCWT
Lena	1.9001	6.5213
Rose	0.4819	4.2187
Cameraman	0.4472	2.9687

Images Results:

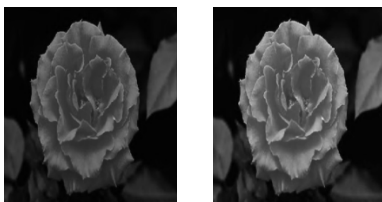
Reconstructed image- Lena



DWT

DTCWT

Reconstructed image- Rose



DWT

DTCWT

Reconstructed image- Cameraman



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References:

- [1] Said, A., and Pearlman, W. A., "A New, Fast, Set Partitioning in Hierarchical Trees", IEEE Transactions Circuits and Systems on Video Technology, Vol. 6, No. 3, pp. 243-250, 1996
- [2] Ahmed Abu Hajar and Ravi Sankar, "Wavelet based Lossless Image Compression using Partial SPIHT and Bit Plane based Arithmetic Coding", 0-7803-7402-9/02, IEEE, 2002
- [3] Mark Johnson, Prakash Ishwar, Vinod Prabhakaran, Daniel Schonberg and Kannan Ramchandran "On Compressing Encrypted Data" IEEE Transactions on Signal Processing, VOL. 52, NO. 10, October 2004
- [4] J. Mal, P. Rajmic, "DWT-SPIHT IMAGE CODEC IMPLEMENTATION", published -2004
- [5] Ramin Eslami and Hayder Radha, "Wavelet-based Contourlet Coding Using an SPIHT-like Algorithm", published -2004
- [6] Ivan W. Selesnick, Richard G. Baraniuk, "The Dual-Tree Complex Wavelet Transform", IEEE Signal Processing magazine, pp123-151, November 2005
- [7] James E. Fowler, Joseph B. Boettcher and B'eatrice Pesquet-Popescu "Image Coding using Complex Dual-Tree Wavelet Transform" 15th European Signal Processing Conference (EUSIPCO 2007), ©2007 EURASIP
- [8] Chuo-Ling Chang and Bernd Girod, "Direction-Adaptive Discrete Wavelet Transform for Image



Compression”, IEEE Transactions on Image Processing, VOL. 16, NO. 5, MAY 2007

[9] Jun-Ren Ding and Jar-Ferr Yang, “A simplified SPIHT Algorithm” , Journal of the Chinese Institute of Engineers, Vol. 31, No. 4, pp. 715-719, 2008

[10] Li Hui Fang Miao Guo Feng Xu Hou Jie, “Images Compression Using Dual Tree Complex Wavelet Transform”, 978-0-7695-4132-7/IEEE , 2010

[11] R.Arokia Priya, S.PNarote, and A.V.Patil “Dual Tree Wavelet Transforms in Image Compression” International Journal of ISSN 0974-2107 Systems and Technologies, Vol.3, No.1, pp 83-95/IJST2010

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